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ZJU-CSE Summer School

Distributed Load Frequency Control in Smart Grid

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- Assistant Professor, DoE, Carleton
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- TC Member, IEEE IES Resilience and Security for Industrial Applications (ReSia)
- Keynote Speaker, Intl.Con.2MAE, 2017, May, Beijing, China
- Session Chairs, IEEE IES ISIE 2021

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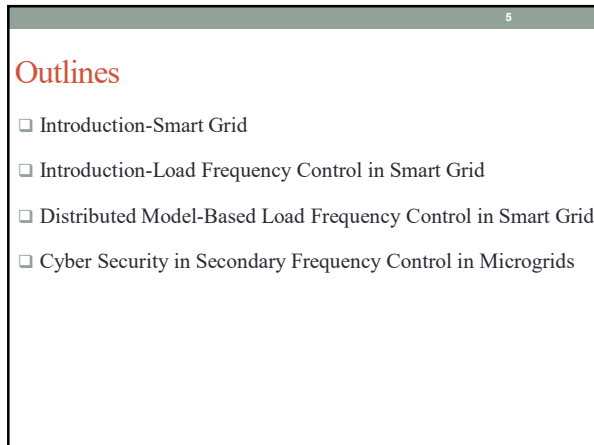
Ottawa



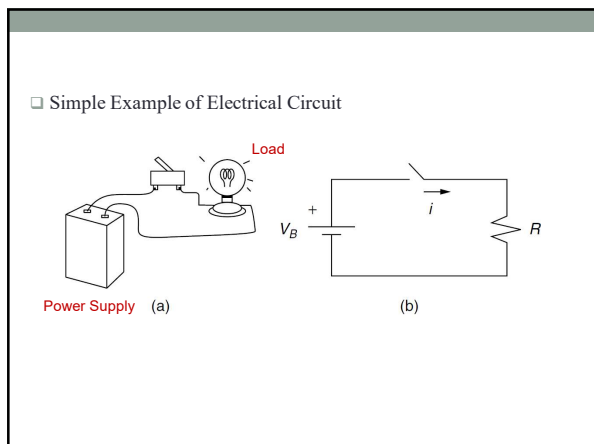
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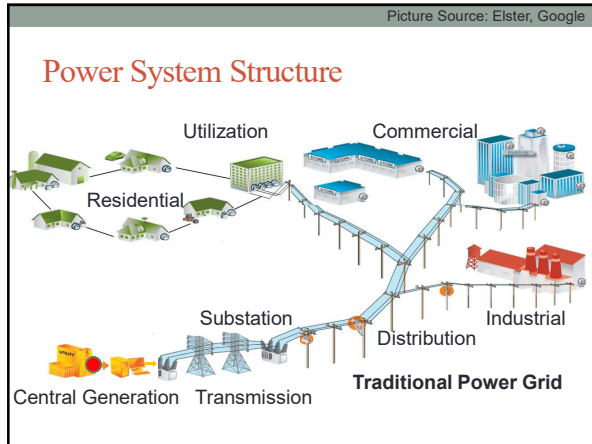
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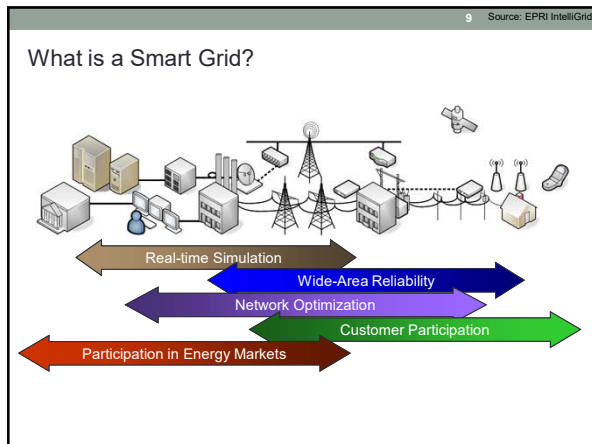
Picture Source: Elster, Google

Northeast Blackout – August 14, 2003

- Affected 55 million people
- \$6 billion lost

US: Per year \$135 billions lost for power interruption

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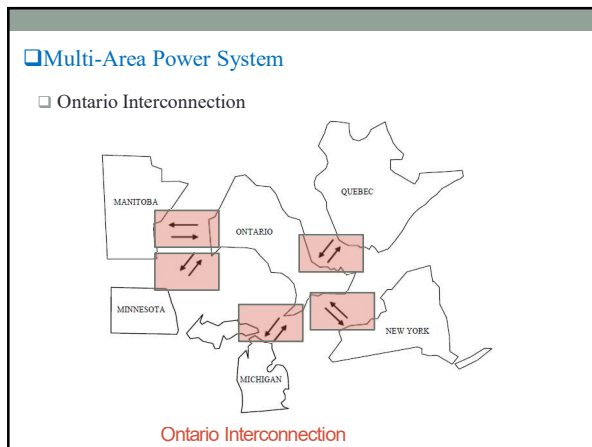


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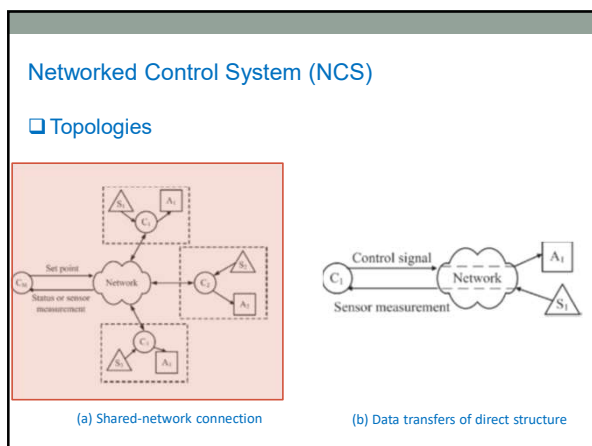
Comparisons

Traditional Power Grid	Smart Grid
Centralized Generation	Distributed Generation
Hierarchical	Networked
One-Way Communication	Two-Way Communication
Manual Restoration	Self-Healing
Few Customer Choices	Many Customer Choices
Limited Control	Pervasive Control

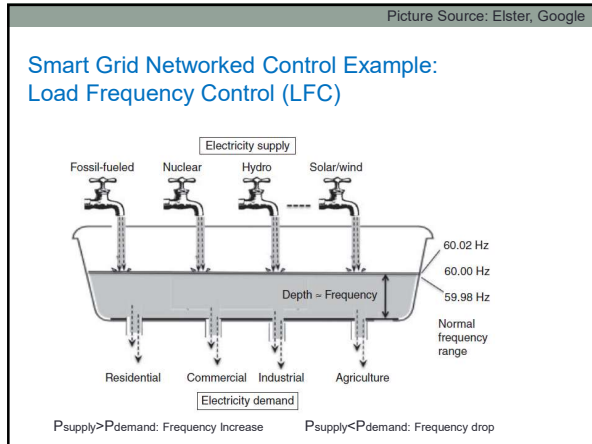
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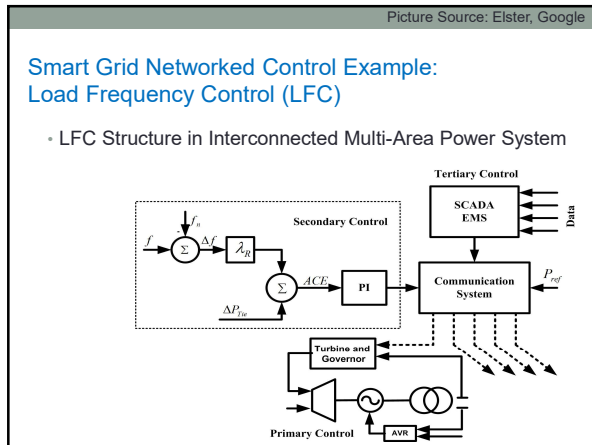
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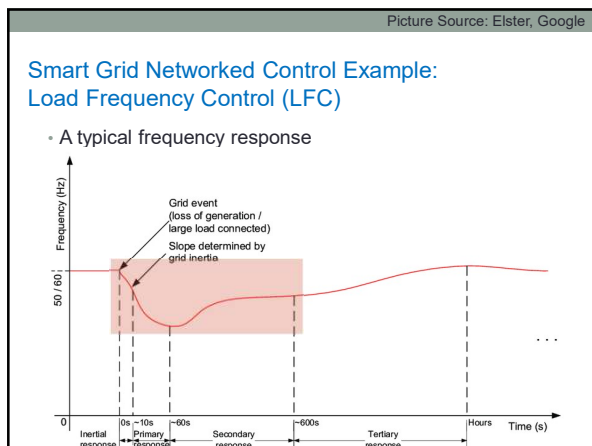
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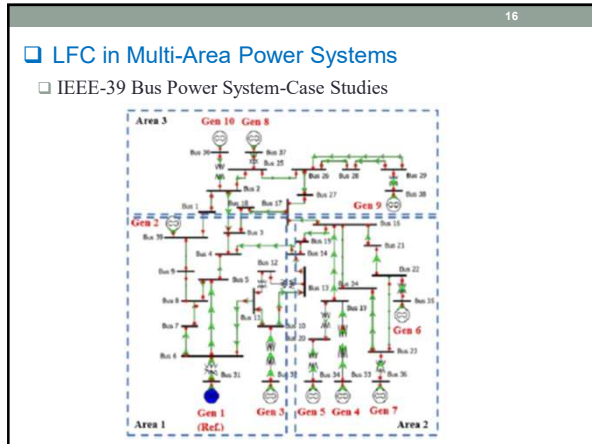
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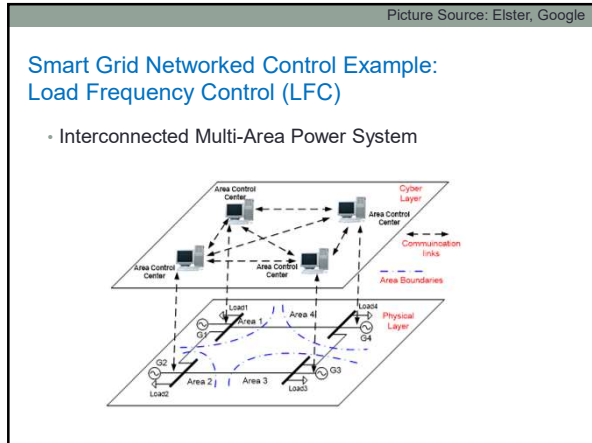
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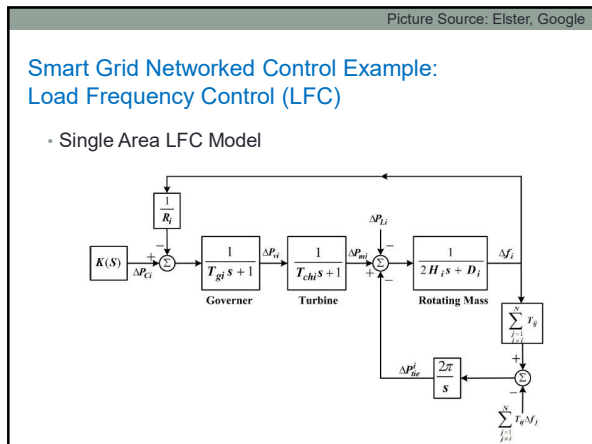
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Picture Source: Elster, Google

Smart Grid Networked Control Example: Load Frequency Control (LFC)

- Challenges: Unreliable factors of communication links involved in LFC of Smart Grid
 - Communication Delays
 - Communication Failures
 - Limited Bandwidth
 - Cyber Attacks
- Questions need to be answered
 - How do these communication-related factors affect LFC of a smart grid?
 - How to compensate the performance degradation of a smart grid due to these communication-related factors?

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Smart Grid Networked Control Example: Load Frequency Control (LFC)

- Study 1: Limited Bandwidth

Four area power systems

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Smart Grid Networked Control Example: Load Frequency Control (LFC)

- Study 1: Limited Bandwidth in Shared Communications

Power System Model of Area i

$$x_i(k+1) = (A_i + \Delta A_i)x_i(k) + B_i u_i(k) + \sum_{j=1, j \neq i}^n A_{ij} x_j(k) + F_i w_i(k)$$

$$y_i(k) = C_i x_i(k)$$

$$u_i(k) = K_i \hat{x}_i(k) + \sum_{j=1, j \neq i}^n K_{ij} \hat{x}_j(k)$$

$$\hat{x}_i(k+1) = A_i \hat{x}_i(k) + B_i u_i(k) + L_i (y_i(k) - C_i \hat{x}_i(k)) + F_i w_i(k)$$

S. Liu et al., "Distributed Model-Based Control and Scheduling for LFC of Smart Grids Over Limited Bandwidth Networks," *IEEE Transactions on Industrial Informatics*, vol. 14, no. 5, pp. 1814-1823, May 2018

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**Smart Grid Networked Control Example:
Distributed Load Frequency Control (LFC)**

• Study 1: Limited Bandwidth in Shared Communications

The sampled discrete-time model for i th area with $i \in \{1, \dots, n\}$ is:

$$\begin{cases} x_i(k+1) &= (A_i + \Delta A_i)x_i(k) + B_i u_i(k) \\ &+ \sum_{j=1, j \neq i}^n A_{ij} x_j(k) + F_i \Delta P_{L_i} \\ y_i(k) &= C_i x_i(k) \end{cases} \quad (7)$$

where, $A_i = e^{A_i^c q}$, $A_{ij} = e^{A_{ij}^c q}$, $\Delta A_i = e^{\Delta A_i^c q}$, $B_i = \int_0^q e^{A_i^c \tau} B_i^c d\tau$, $C_i = C_i^c$, $F_i = \int_0^q e^{A_i^c \tau} F_i^c d\tau$ and q is the sampling period.

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**Smart Grid Networked Control Example:
Distributed Load Frequency Control (LFC)**

• Study 1: Limited Bandwidth in Shared Communications

In i th area, the following distributed model-based controller is designed

$$u_i(k) = K_i \hat{x}_i(k) + \sum_{j=1, j \neq i}^{n_i} K_{ij} \hat{x}_j(k), i \in \{1, 2, \dots, n\} \quad (9)$$

$$\begin{cases} \hat{x}_i(k+1) &= A_i \hat{x}_i(k) + B_i u_i(k) \\ &+ \sum_{j=1, j \neq i}^{n_i} A_{ij} \hat{x}_j(k) + F_i \Delta P_{L_i}, k \neq t_k \\ \hat{x}_j(k+1) &= A_j \hat{x}_j(k) + B_j \hat{u}_j(k) \\ &+ \sum_{r=1, r \neq j}^{n_j} A_{jr} \hat{x}_r(k) + F_j \Delta P_{L_j}, k \neq t_k \\ \hat{u}_j(k) &= K_j \hat{x}_j(k) + \sum_{r=1, r \neq j}^{n_j} K_{jr} \hat{x}_r(k) \\ \hat{x}_j(t_k) &= \bar{x}_j(t_k), j \in \{1, \dots, n_i\}, k = t_k \end{cases} \quad (10)$$

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**Smart Grid Networked Control Example:
Distributed Load Frequency Control (LFC)**

• Study 1: Limited Bandwidth in Shared Communications

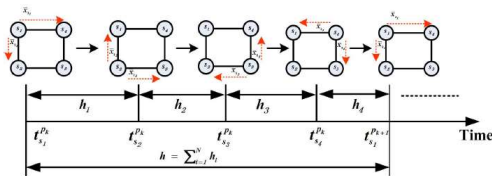
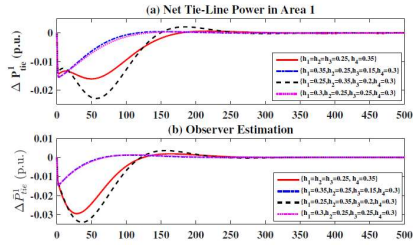


Illustration of the RTU broadcasting schedule

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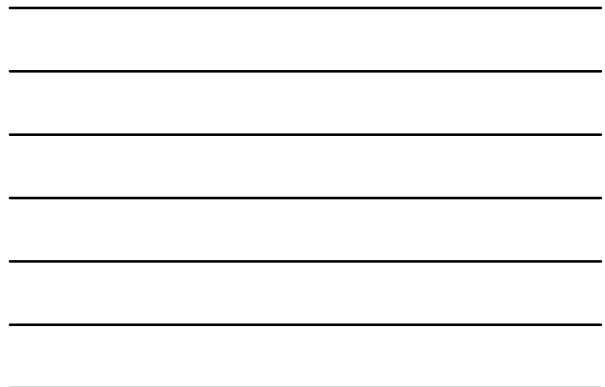
Smart Grid Networked Control Example: Distributed Load Frequency Control (LFC)

• Study 1: Limited Bandwidth in Shared Communications



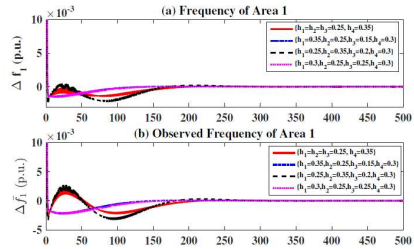
System dynamics under various broadcasting interval settings

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Smart Grid Networked Control Example: Distributed Load Frequency Control (LFC)

• Study 1: Limited Bandwidth in Shared Communications



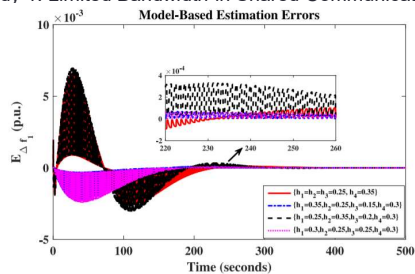
System dynamics under various broadcasting interval settings

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Smart Grid Networked Control Example: Distributed Load Frequency Control (LFC)

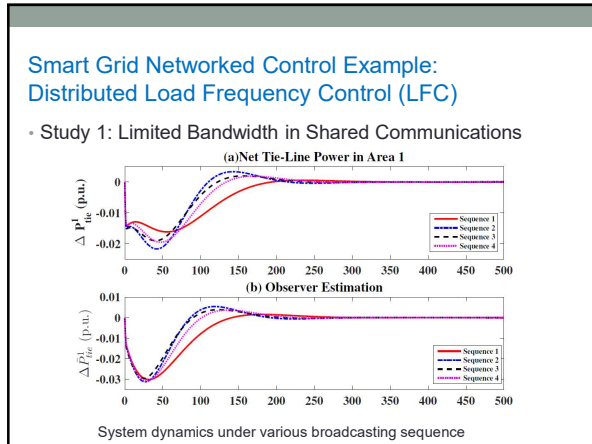
• Study 1: Limited Bandwidth in Shared Communications



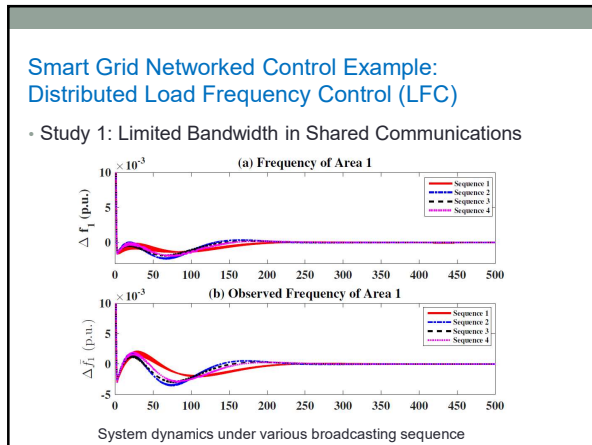
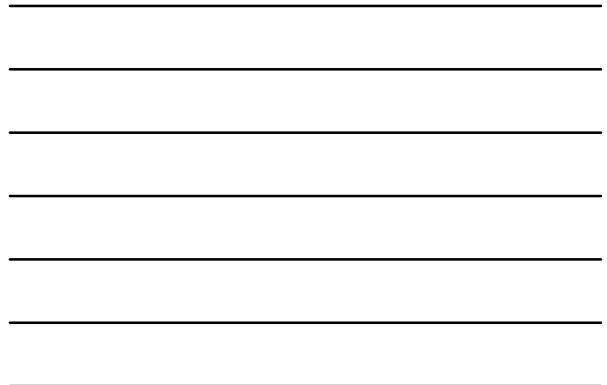
System dynamics under various broadcasting interval settings

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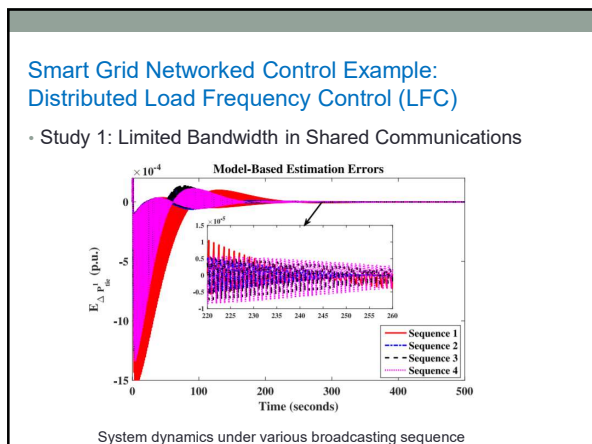




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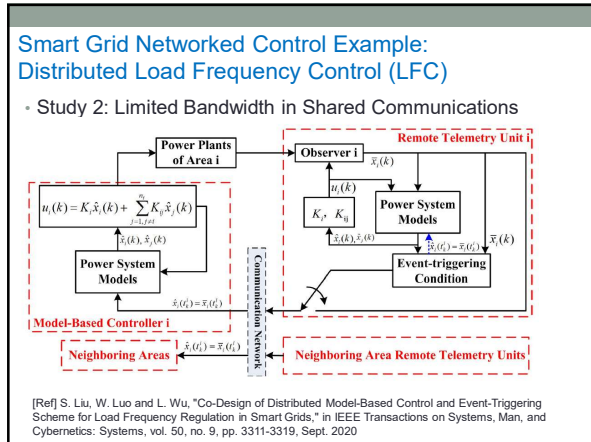


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Smart Grid Networked Control Example: Distributed Load Frequency Control (LFC)

• Study 2: Limited Bandwidth in Shared Communications

Event-Triggering Condition

$$b\|\hat{e}_i(k)\|_2^2 \leq a\|x_i(k)\|_2^2$$

where $\hat{e}_i(k) = \bar{x}_i(k) - \hat{x}_i(k)$ denotes the prediction error between the state observation $\bar{x}_i(k)$ and $\hat{x}_i(k)$ which is the state estimated based on the power system model in the RTU, and a and b are scalars to be designed in terms of the event-triggering mechanism.

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Smart Grid Networked Control Example: Distributed Load Frequency Control (LFC)

• Study 2: Limited Bandwidth in Shared Communications

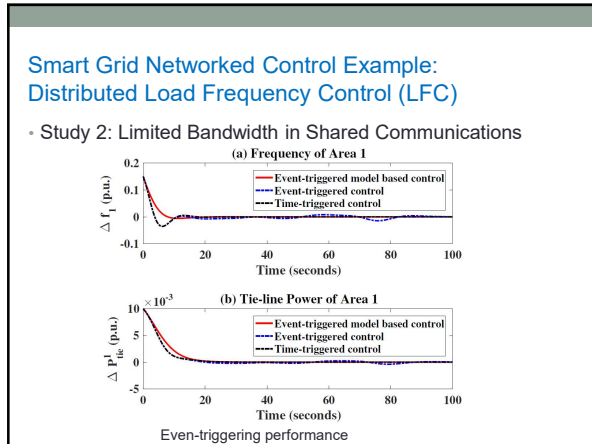
Event-Triggering Condition: $b\|\hat{e}_i(k)\|_2^2 \leq a\|x_i(k)\|_2^2$

Theorem 1: Given positive constants ϵ, β , the uncertain power system (12) is ISS if there exist positive definite matrices P_1, P_2 , and matrices $Q_1 > 0, Q_2 > 0, M \in R^{2n \times 2n}, N \in R^{2n \times 2n}$, such that the LMI (as show at the top of the next page) holds, where $P_1 = U_1^T P_{11} U_1 + U_2^T P_{22} U_2$. The controller gain $K = V \Sigma^{-1} P_{11}^{-1} \Sigma V^T M$, the observer gain $L = P_2^{-1} N$ if

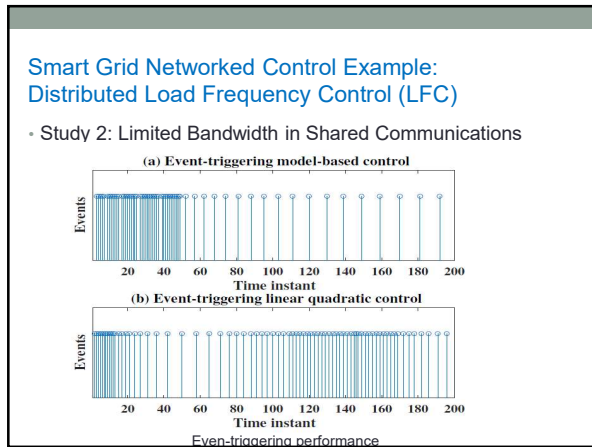
$$b\|\hat{e}(k)\|_2^2 \leq a\|x(k)\|_2^2 \quad (21)$$

where $-a = -\lambda_{\min}(Q) + \beta\|\Phi\|_2^2$ and $b = \beta^{-1}\|P\|_2^2\|\Gamma\|_2^2 + \|P\|_2\|\Gamma\|_2^2$.

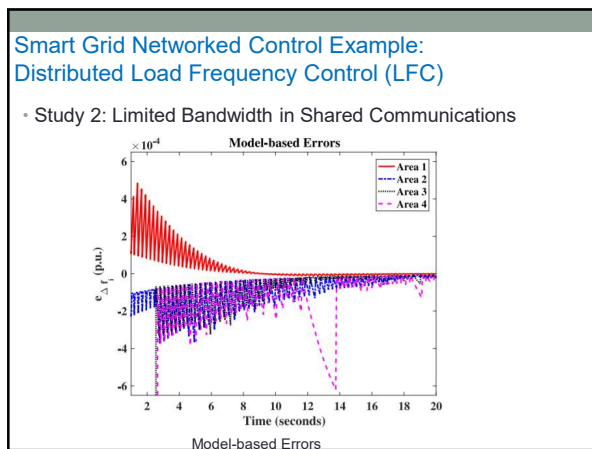
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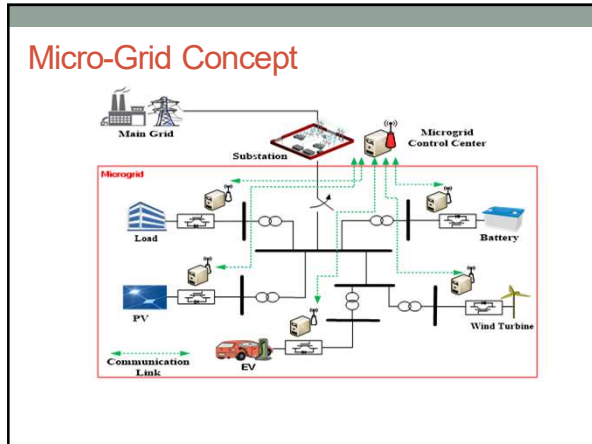


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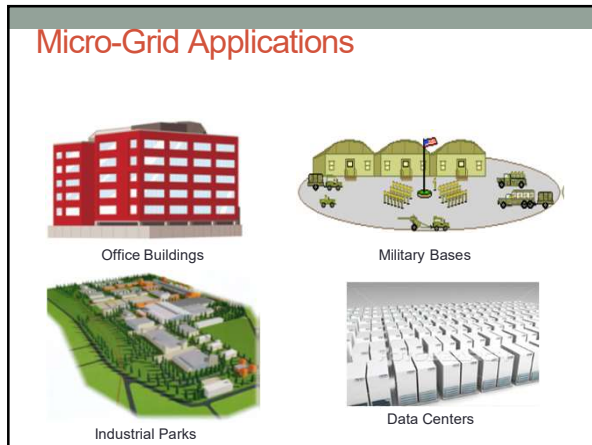


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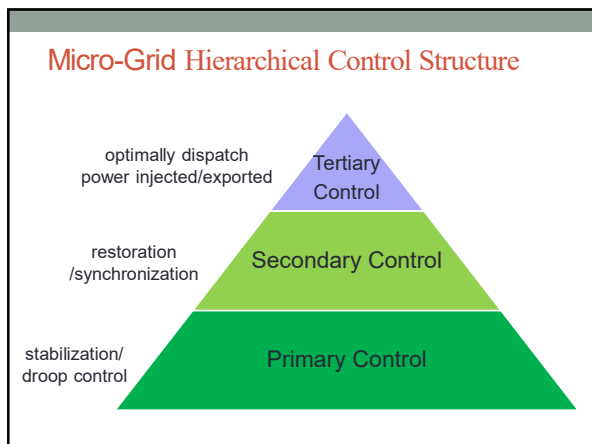




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Micro-Grid Droop Control

$f = f_0 - k_p(P - P_0)$

$V_1 = V_0 - k_v(Q - Q_0)$

An experimental study of frequency droop control in a low-inertia microgrid, Andrew Bollman

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Resynchronization of Islanded Microgrid

- Function of a resynchronization controller
 - Ensure smooth reconnection of microgrid and main grid
 - Restore the nominal frequency
 - Two kinds of control strategies
 - Centralized controller
 - Distributed controller

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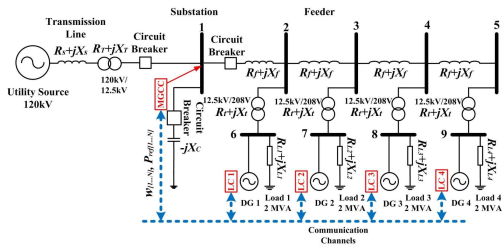
Secondary Frequency Control

- Basic Principle

secondary frequency control, Alireza Raghani

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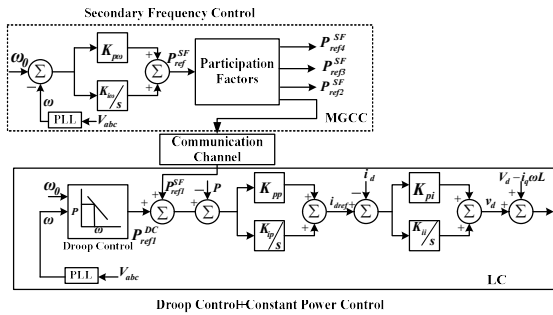
Secondary Frequency Control



S. Liu, X. Wang and P. X. Liu, "Impact of Communication Delays on Secondary Frequency Control in an Isolated Microgrid," in *IEEE Transactions on Industrial Electronics*, vol. 62, no. 4, pp. 2021-2031 April 2015

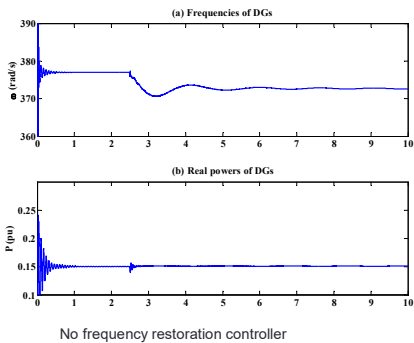
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Secondary Frequency Control

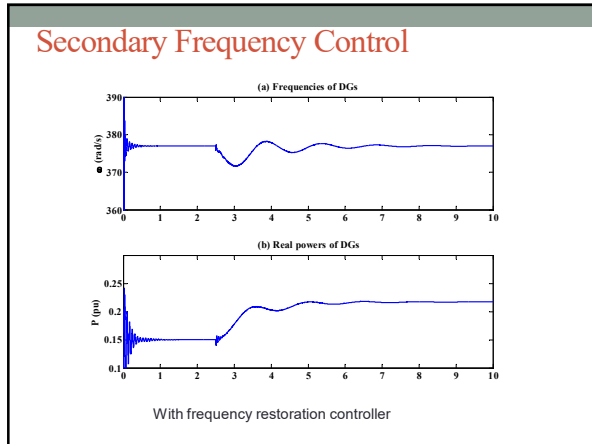


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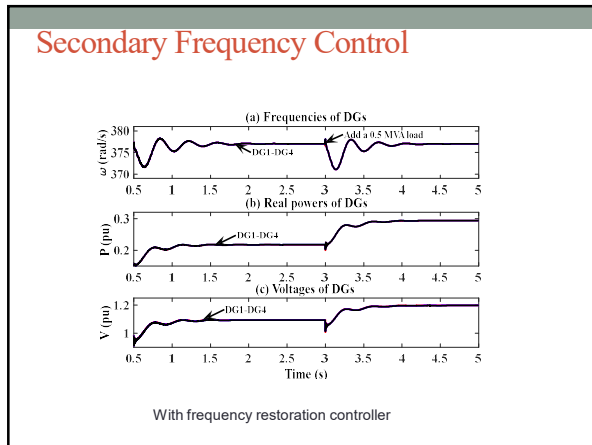
Secondary Frequency Control



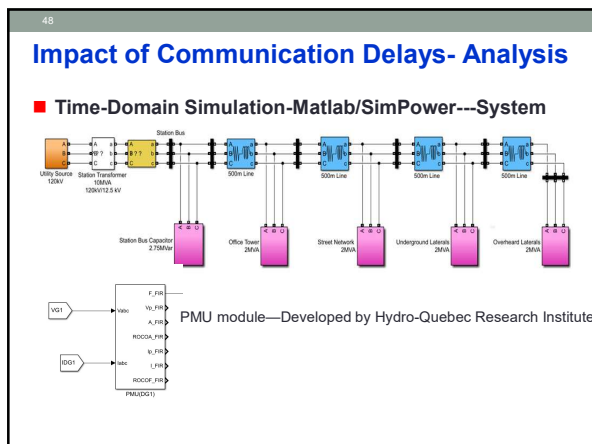
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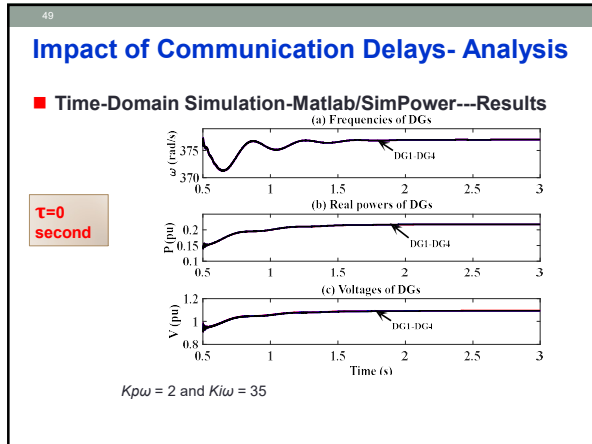
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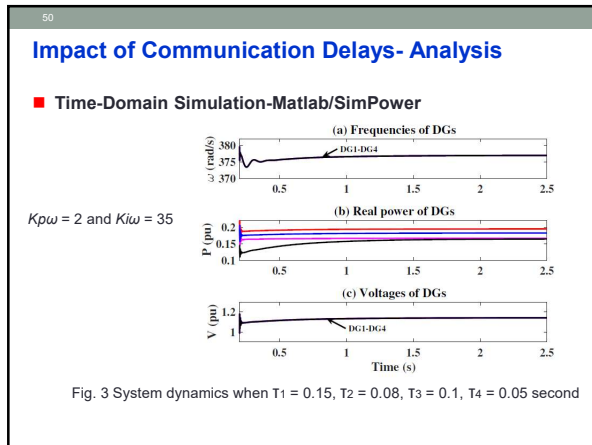
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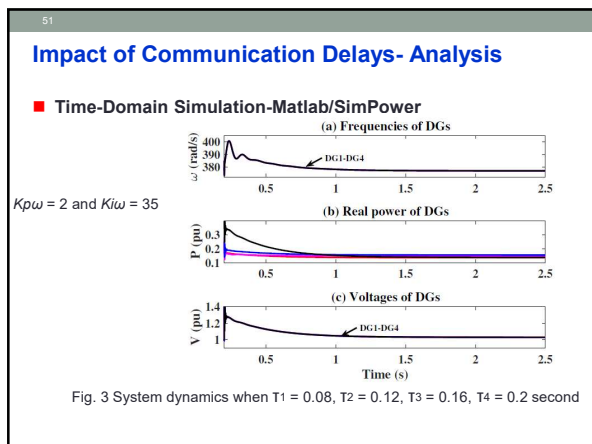
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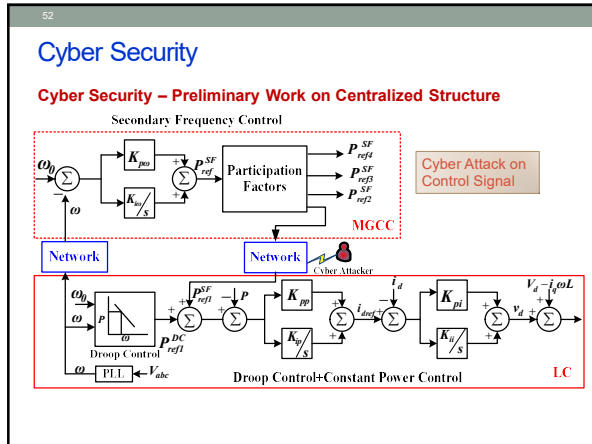
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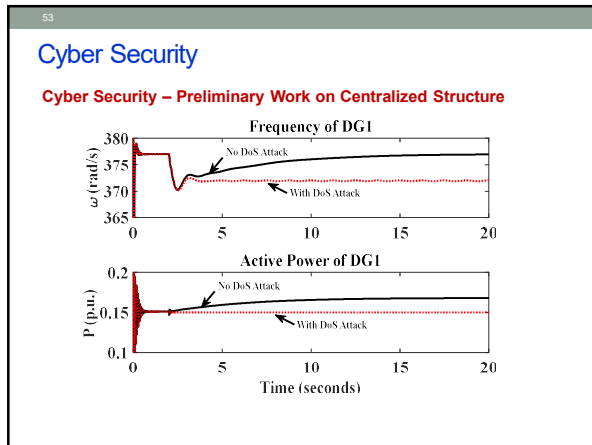
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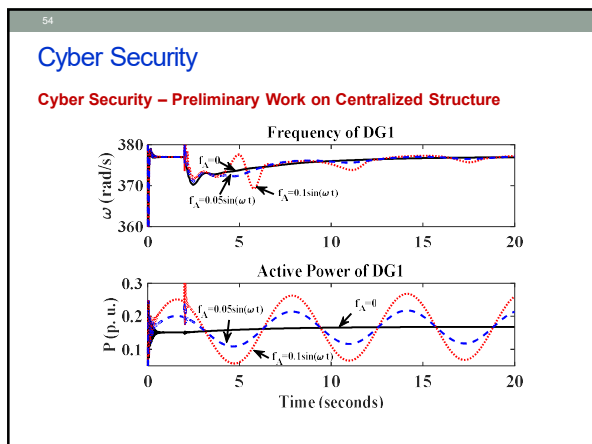
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